

# Regret theory and risk attitudes

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**Abstract** We examine risk attitudes under regret theory and derive analytical expressions for two components—the resolution and regret premiums—of the risk premium under regret theory. We posit that *regret*-averse decision makers are risk seeking (resp., risk averse) for low (resp., high) probabilities of gains and that feedback concerning the foregone option reinforces risk attitudes. We test these hypotheses experimentally and estimate empirically both the resolution premium and the regret premium. Our results confirm the predominance of regret aversion but not the risk attitudes predicted by regret theory; they also clarify how feedback affects attitudes toward both risk and regret.

**Keywords** Regret theory · Resolution premium · Regret premium · Regret aversion

**JEL Classification** D81

### 1 Introduction

In economics and management, the classic model of expected utility (von Neumann and Morgenstern 1947) is the benchmark for representing preferences under risk and uncertainty. Yet several models have been introduced since the 1970s to accommodate

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some of expected utility's descriptive failures (for reviews see Starmer 2000; Wakker 2010). Regret theory (Bell 1982; Loomes and Sugden 1982) is one of the most popular alternatives to expected utility (EU). Regret theory is based on the intuition that a decision maker (DM)—when choosing among risky objects (e.g., lotteries, gambles, and investments)—is concerned not only about the payoff he receives but also about the foregone payoff, i.e., had he chosen differently. Regret theory has a simple structure: a utility function capturing attitudes toward outcomes and a function capturing the effect of regret. Despite this structural simplicity, regret theory can account for many of the empirical violations of EU (Loomes and Sugden 1982). The key to explaining these violations is the psychological intuition that most decision makers are by nature regret averse. Regret theory's intuitive content and explanatory power make it well suited to real-world applications. For example, Barberis and Thaler (2006), Gollier and Salanié (2006), Muermann and Volkman (2006), Michenaud and Solnik (2008), and Qin (2015) have applied the notion of regret to financial and insurance decisions. Perakis and Roels (2008) reinterpreted the newsvendor model in terms of regret, and Filiz-Ozbay and Ozbay (2007) and Engelbrecht-Wiggans and Katok (2008) proposed models in auction theory that rely on regret. Diecidue and Tang (2012), Nasiry and Popescu (2012), and Viefers and Strack (2014) focused on dynamic applications of regret.

To deploy regret theory for decision analysis, the risk attitudes under that theory should be well understood. Under EU, risk attitudes are fully captured by "utility curvature" (Wakker 2010); in more complex models, such as prospect theory (Kahneman and Tversky 1979; Tversky and Kahneman 1992; Tversky and Wakker 1995), risk attitudes are captured by the interaction between utility and a probability weighting function that yields a fourfold pattern of risk attitudes. Under regret theory, however, it is not clear how the interaction between utility and regret is related to risk attitudes. Bell (1983) formalized the risk premium under regret theory and showed that it consists of two distinct components: a resolution premium and a regret premium. However, Bell (1983) did not suggest an empirical method suitable for measuring these two components (Anand 1985).

In this paper, we provide an analytical expression for both the resolution premium and the regret premium. These expressions enable—for the first time—a precise characterization of risk attitudes under regret theory and thus rigorous predictions about the risk attitudes of a regret-averse decision maker. We predict that regret-averse DMs will be risk seeking for low probabilities of gains and risk averse for high probabilities; we also postulate that risk attitudes are reinforced by feedback about the foregone payoff. We introduce a method to measure the risk premium under regret theory. This method allows us then to compute both the resolution and regret premiums and thereby to understand the effect of feedback on regret attitudes. Finally, we design an experiment to estimate empirically the risk premium's components and to test our predictions about risk attitudes. The experiment serves also as a descriptive test of regret theory.

<sup>&</sup>lt;sup>1</sup>The role of regret in the psychology of decision making has been extensively investigated (Larrick 1993; Larrick and Boles 1995; Zeelenberg 1999; Connolly and Zeelenberg 2002; Connolly and Butler 2006).



The data support regret aversion as a robust empirical phenomenon. However, we find no significant support for the risk attitude predictions of regret theory. We also discover that immediate feedback polarizes regret attitudes: It increases the regret aversion of regret-averse subjects but it reduces the regret aversion within the entire subject pool.

The paper is organized as follows. Section 2 introduces the notation and the definition of regret theory; in Section 3, we first derive analytically the two components of the risk premium under regret theory and then introduce a measurement that distinguishes the two components. Building on this new measurement, Section 4 derives formal predictions for the risk attitudes of a regret-averse decision maker; the experiment described in Section 5 tests those predictions. We discuss the experiment's results and conclude in Section 6.

## 2 Notation and basic concepts

Regret theory considers the utility of the outcomes associated with the selected prospect and also the regret or "rejoicing" associated with comparisons between the selected and the foregone prospect. Before defining regret theory formally, we examine some of its basic formulations and properties. Consider the two-outcome prospects  $\alpha_E \beta$  and  $\gamma_E \delta$ . The general formulation of regret theory proposed by Loomes and Sugden (1987) postulates a real-valued function  $\psi$  such that

$$\alpha_E \beta \succeq \gamma_E \delta \iff p \psi(\alpha, \gamma) + (1 - p) \psi(\beta, \delta) \ge 0.$$
 (1)

The function  $\psi(\alpha,\gamma)$  can be interpreted as assigning a real-valued index to the net advantage of choosing  $\alpha_p\beta$  rather than  $\gamma_p\delta$  if event E obtains with subjective probability p. The function  $\psi$  is unique up to scale—that is, it can be replaced by any other function  $\psi'=a\psi$  without affecting preferences—and satisfies the following two restrictions.

- 1. The function  $\psi$  is *strictly increasing* (resp., *strictly decreasing*) in its first (resp., second) argument: for any outcome  $\gamma$ , if  $\alpha > \beta$  then  $\psi(\alpha, \gamma) > \psi(\beta, \gamma)$  and  $\psi(\gamma, \alpha) < \psi(\gamma, \beta)$ .
- 2. The function  $\psi$  is skew symmetric: for all  $\alpha$  and  $\beta$ ,  $\psi(\alpha, \beta) = -\psi(\beta, \alpha)$ .



Bell (1982) and Loomes and Sugden (1982) considered a restricted form of Eq. 1 in which

$$\psi(\alpha, \beta) = Q(u(\alpha) - u(\beta)), \tag{2}$$

where Q is the regret function and u is a von Neumann–Morgenstern utility function.<sup>2</sup> We use Eq. 2 to define regret theory formally as follows.

**Definition 1** *Regret theory* holds if there exist both a continuous strictly increasing utility function  $u: \mathbb{R} \to \mathbb{R}$  and a continuous strictly increasing skew-symmetric regret function  $Q: \mathbb{R} \to \mathbb{R}$  such that

$$f \succeq g \iff \sum_{i=1}^{n} p_i \cdot Q(u(f_i) - u(g_i)) \ge 0; \tag{3}$$

here  $f = (E_1, f_1; ...; E_n, f_n)$  and  $g = (E_1, g_1; ...; E_n, g_n)$  are prospects and  $p_i$  is the subjective probability of event  $E_i$ . The skew-symmetry of Q implies  $Q(\alpha) = -Q(-\alpha)$  for any outcome  $\alpha$ .

Expected utility is the special case of Eq. 3 in which Q is the identity function. The convexity (resp., concavity) of the Q-function indicates regret aversion (resp., regret seeking). Regret aversion is responsible for the distinctive predictions of regret theory (see Loomes and Sugden 1982; Bleichrodt and Wakker 2015). Bleichrodt and Diecidue (2010) presented the first quantitative (non parametric) measurement of Eq. 3, i.e., allowed to measure utility u and regret function Q at the individual level.

Definition 1 illustrates the behavior of a DM that compares the outcomes of the chosen prospect with those of the foregone prospect, state by state. Therefore, if the DM receives feedback about the chosen and foregone prospect (post choice), then the possibility of regret—receiving a lower outcome compared to the foregone prospect —becomes more salient to the DM. We conjecture that this makes the DM likely to engage more intensely in such state by state outcome comparisons before choosing. The intuition is supported by the psychological research: Larrick and Boles (1995), Zeelenberg et al. (1996), Zeelenberg and Beattie (1997), and Zeelenberg (1999) have shown that systematic effects of anticipated regret are observed in conditions—like immediate feedback—where the possibility of regret is made highly salient to the DM. Therefore feedback seems to enhance anticipated regret. However, regret theory —as in Definition 1—does not incorporate feedback. To provide a thorough analysis of risk attitudes under regret theory, it is therefore required to include feedback into Eq. 3. For this purpose, we consider two variants of Eq. 3: the first variant uses a regret function  $Q_N$  to capture "pure" anticipated regret with **No feedback**, while the second variant uses a regret function  $Q_F$  to capture anticipated regret when **Feedback** is available. Therefore, by comparing the regret functions under feedback  $(Q_F)$ and no feedback  $(Q_N)$ , we can understand the effect of feedback on anticipated regret and choices. Larrick and Boles (1995) and Zeelenberg (1999) have shown that resolving the foregone option and providing immediate feedback increases regret aversion.

 $<sup>^{2}</sup>$ Loomes and Sugden (1982) refer to u as a "choiceless utility function".



As the DM becomes more regret averse, the Q function becomes more convex. We therefore expect  $Q_F$  to be more convex than  $Q_N$ . We validate this assumption later in our experiment.

## 3 Risk premium under regret: Derivation

The *risk premium* of a prospect is the monetary difference between its expected value (EV) and the sure amount (the certainty equivalent CE) that makes the decision maker indifferent to that prospect. The risk premium (RP) under regret theory is the difference between the EV and the CE of the prospect under regret theory. To provide a complete characterization of risk premium under regret theory, we focus on the regret theory variant under feedback. In this case, the risk premium is  $RP = EV - CE_{RT_F}$ , where  $CE_{RT_F}$  is the certainty equivalent under regret theory with feedback. Given the certainty equivalent under regret theory with no feedback ( $CE_{RT_N}$ ) and certainty equivalent under expected utility ( $CE_{EU}$ ), the risk premium under regret theory with feedback (RP) can be rewritten as follows:

$$RP = (CE_{RT_N} - CE_{RT_F}) + (CE_{EU} - CE_{RT_N}) + (EV - CE_{EU}).$$
 (4)

The first component  $(CE_{RT_N} - CE_{RT_F})$  is the *resolution premium*. This entails that the DM is not indifferent to "resolving" the foregone option: the premium is the amount a DM pays to avoid the resolution of the foregone option. The convexity of  $Q_F$  compared to  $Q_N$  determines the resolution premium. The second component  $(CE_{EU} - CE_{RT_N})$  is the *regret premium*, i.e., is the extra amount that a DM pays to avoid regret as compared to an EU maximizer. The convexity of  $Q_N$  and the concavity of  $Q_N$  determine the regret premium. The third component  $(EV - CE_{EU})$  is the risk premium under expected utility. The concavity of utility function  $Q_N$  determines the risk premium under EU.

To provide intuition for Eq. 4, consider a DM facing choices 1 and 2 in Table 1. Assume the four events  $E_1$ ,  $E_2$ ,  $E_3$ , and  $E_4$  are equally likely; as a consequence f and g, f' and g' have the same expected value. Suppose the DM prefers prospect f to g and receives nothing after the uncertainty is resolved (e.g., event  $E_4$  turns up). The DM will regret the decision: not only did he receive \$0, but he also lost the opportunity to earn a sure amount of \$15,000. The premium a DM is willing to pay in order to avoid regret is the *regret premium*.

**Table 1** Choice between prospects

	$E_1$	$E_2$	$E_3$	$E_4$
Choice 1				
f	\$ 20k	\$ 20k	\$ 20k	0
g	\$ 15k	\$ 15k	\$ 15k	\$ 15k
Choice 2				
f'	\$ 40k	0	0	0
g'	\$ 20k	\$20k	0	0



Suppose the DM prefers prospect f' to g' and then—after resolution of the uncertainty—receives nothing. The DM might (or might not) like to hear about the outcomes of prospect g'. The amount of money a DM will pay to avoid (hearing about) resolution of the foregone prospect is the *resolution premium*.<sup>3</sup>

In the rest of this section we derive analytical expressions for the risk premium components under regret theory as in Eq. 1.

**Resolution premium** Consider prospects of the form  $x = (p, x_k; 1 - p, x_0)$ ; here  $p \in (0, 1)$  and  $x_k \ge x_0 \ge 0$ . The resolution premium (ResP) of a prospect x is the difference between  $CE_{RT_N}$  and  $CE_{RT_F}$ ; it is derived in Online Appendix C and is given by

$$\operatorname{ResP}(x) = C E_{RT_N} - C E_{RT_F} = u^{-1} \left( u(x_k) \left( \frac{Q_N^{-1} \left( \frac{p}{1-p} \right)}{1 + Q_N^{-1} \left( \frac{p}{1-p} \right)} \right) \right) - u^{-1} \left( u(x_k) \left( \frac{Q_F^{-1} \left( \frac{p}{1-p} \right)}{1 + Q_F^{-1} \left( \frac{p}{1-p} \right)} \right) \right).$$
 (5)

Replacing  $Q_F$  and  $Q_N$  in Eq. 5 with the power function specifications  $Q_F(\alpha) = \alpha^{\theta_1}$  and  $Q_N(\alpha) = \alpha^{\theta_2}$ , we obtain

$$\operatorname{ResP}(x) = C E_{RT_N} - C E_{RT_F} = u^{-1} \left( u(x_k) \left( \frac{\left(\frac{p}{1-p}\right)^{1/\theta_2}}{1 + \left(\frac{p}{1-p}\right)^{1/\theta_2}} \right) \right) - u^{-1} \left( u(x_k) \left( \frac{\left(\frac{p}{1-p}\right)^{1/\theta_1}}{1 + \left(\frac{p}{1-p}\right)^{1/\theta_1}} \right) \right).$$

Here  $\theta$  captures the convexity of Q function, and thereby regret aversion.

**Regret premium** The regret premium (RegP) for prospect x is the difference between the certainty equivalent under EU ( $CE_{EU}$ ) and the CE under regret with no feedback ( $CE_N$ ), where the latter is derived in Online Appendix C. Hence, we can write the regret premium (RegP) of prospect x as

$$\operatorname{RegP}(x) = u^{-1} \left( u(x_k) \cdot p \right) - u^{-1} \left( u(x_k) \left( \frac{Q_N^{-1} \left( \frac{p}{1-p} \right)}{1 + Q_N^{-1} \left( \frac{p}{1-p} \right)} \right) \right). \tag{6}$$

<sup>&</sup>lt;sup>3</sup>If instead the DM does want to hear about (resp., is indifferent to) the foregone prospect's payoffs, then the resolution premium is negative (resp., zero).



Replacing  $Q_N$  in Eq. 6 with the power function specification  $Q_N(\alpha) = \alpha^{\theta_2}$ , we obtain

RegP(x) = 
$$u^{-1} (u(x_k) \cdot p) - u^{-1} \left( u(x_k) \left( \frac{\left(\frac{p}{1-p}\right)^{1/\theta_2}}{1 + \left(\frac{p}{1-p}\right)^{1/\theta_2}} \right) \right).$$

**Risk premium under expected utility** The risk premium under expected utility  $(RP_{EU})$  for the prospect x is the difference between the expected value (EV) of the prospect and the certainty equivalent under expected utility  $(CE_{EU})$ :

$$RP_{EU}(x) = p \cdot x_k + (1 - p)x_0 - u^{-1}(p \cdot u(x_k)). \tag{7}$$

Note that, for any two-outcome prospect  $x = (p, x_k; 1 - p, x_0)$ , the term  $u(x_0)$  can be scaled to 0 and the risk premium under expected utility can be computed using Eq. 7.

## 4 Risk attitudes under regret

According to the results presented in Section 3, the risk premium of prospect x under regret is the sum of resolution premium, regret premium, and risk premium under expected utility (ResP(x) + RegP(x) +  $RP_{EU}(x)$ ). Larrick and Boles (1995) and Zeelenberg et al. (1996) provided experimental evidence that a regret-averse decision maker could be both risk averse and risk seeking without any further characterization. Given that we have derived expressions for the components of risk premium under regret, in this section we present a result that characterizes the risk attitude of a regret-averse DM—that is, a decision maker described by a convex Q-function. Under regret theory, a DM's risk attitude is reflected mainly by the regret function Q while the utility function u captures attitude toward money. To extract the pure effect of regret on risk attitude, in the following analysis we shall assume that u is linear (thereby  $RP_{EU}$  is assumed to be zero). Previous literature (Fox and Tversky 1996; Lopes and Oden 1999) has documented a linear utility function when the amounts of money involved are moderate. The assumption of linear utility under regret theory was also validated empirically by the estimates of Bleichrodt and Diecidue (2010), and Baillon and Cillo (2015). Under linear utility, the expressions for resolution premium (ResP) and regret premium (RegP) in Eqs. 5 and 6 can be simplified as follows (scaling  $u(x_0) = 0$  yields  $u(x_k) = x_k - x_0$ ):

ResP(x) = 
$$(x_k - x_0) \cdot \left( \left( \frac{Q_N^{-1} \left( \frac{p}{1-p} \right)}{1 + Q_N^{-1} \left( \frac{p}{1-p} \right)} \right) - \left( \frac{Q_F^{-1} \left( \frac{p}{1-p} \right)}{1 + Q_F^{-1} \left( \frac{p}{1-p} \right)} \right) \right),$$
 (8)

$$\operatorname{RegP}(\mathbf{x}) = (x_k - x_0) \cdot \left( p - \left( \frac{Q_N^{-1} \left( \frac{p}{1-p} \right)}{1 + Q_N^{-1} \left( \frac{p}{1-p} \right)} \right) \right). \tag{9}$$



Consider a prospect of the form  $x = (p, x_k; 1 - p, x_0)$ , where  $x_k \ge x_0 \ge 0$ . The following proposition uses Eqs. 8 and 9 to characterize the risk attitudes of a regret-averse decision maker.

**Proposition 1** Suppose regret theory holds with a linear utility function u and a regret function  $Q_F$ . Then a regret-averse DM is risk seeking for probabilities  $p \in (0, 1/2)$ , is risk averse for probabilities  $p \in (1/2, 1)$ , and is risk neutral for probability p = 1/2.

*Proof* The proof (see Online Appendix D) relies on analyzing the resolution and regret premiums for all possible values of probability p (i.e., p = 1/2,  $p \in (0, 1/2)$ , and  $p \in (1/2, 1)$ ). We prove the proposition by showing that both the resolution premium and the regret premium are negative for probabilities  $p \in (0, 1/2)$  yet are positive for probabilities  $p \in (1/2, 1)$ .

Under no feedback—the case of a regret-averse DM with regret function  $Q_N$  and no feedback about resolution of the foregone option—the resolution premium (ResP) is zero and hence the risk premium coincides with the regret premium (RegP). It follows from Proposition 1 that the regret premium is negative for probability  $p \in (0, 1/2)$  and positive for probability  $p \in (1/2, 1)$ . So even in the absence of feedback, a regret-averse DM is risk seeking for p < 1/2 and risk averse for p > 1/2. These risk attitudes are reinforced (because of the resolution premium) when there is feedback, as described in Proposition 1.<sup>4</sup>

If the utility function u is not linear, then the regret-averse DM is still risk seeking for low probabilities of gains and risk averse for high probabilities; however, the risk neutrality cutoff point is no longer p=1/2. In particular, if u is concave (resp., convex) then the DM is risk seeking for probabilities (0, m), m < 1/2 (resp., m > 1/2).

**Resolution and regret premiums:** An example To illustrate the intuition behind Proposition 1, we calculate resolution and regret premiums for a specific example. Following the empirical estimates of Bleichrodt and Diecidue (2010), we assume that  $u(\alpha) = \alpha^{0.96}$  for the utility function and that  $Q_N(\alpha) = \alpha^{1.73}$ . Because  $Q_F$  is expected to be more convex than  $Q_N$ , we assume  $Q_F(\alpha) = \alpha^{3.26}$ —a value in the top decile of the estimates from Bleichrodt et al. (2010). Assuming u(0) = 0, we compute the resolution and regret premiums of the prospect  $(p_j, 100; 1 - p_j, 0)$  for different probabilities  $p_j$ .

Table 2 reports the resolution and regret premiums computed using (respectively) Eqs. 5 and 6. The certainty equivalent of regret theory under no feedback ( $CE_{RT_N}$ ) is computed by adding the regret premium to the CE under EU ( $CE_{EU}$ ); we obtain the CE of regret theory under feedback ( $CE_{RT_F}$ ) by adding the resolution premium to the  $CE_{RT_N}$ . The risk premium, resolution premium, and regret premium are

<sup>&</sup>lt;sup>4</sup>In our set-up, note that the resolution premium is computed independently from the regret premium. So our set-up allows a regret-averse DM to be resolution seeking.

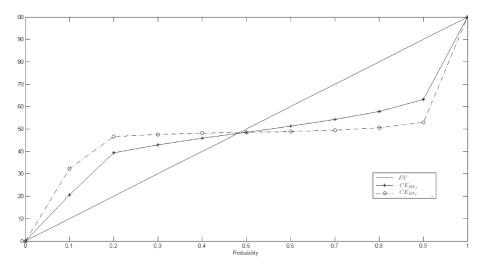


Probability	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
Resolution premium	- 11.68	- 8.53	- 5.56	- 2.75	0	2.77	5.65	8.75	12.16
Regret premium	-11.5	-19.32	-13.52	-6.94	0	7.01	13.83	20.04	24.49
$CE_{EU}$	9.09	18.70	28.53	38.50	48.58	58.74	68.97	79.26	89.61
$CE_{RT_N}$	20.58	39.32	42.87	45.83	48.58	51.33	54.31	57.91	63.14
$CE_{RT_F}$	32.27	46.56	47.62	48.19	48.58	48.95	49.48	50.47	52.95
Total risk premium	- 23.18	-27.85	- 19.09	-9.69	0	9.78	19.48	28.79	36.66

Table 2 Resolution premium and regret premium for a specific example

negative for low probabilities and are positive for high probabilities of gains. This relation indicates that a regret-averse DM is risk seeking for low probabilities of gains and risk averse for high probabilities (under no feedback) and that this attitude is reinforced in the presence of feedback owing to the resolution premium. The intuition for this result is as follows. If a DM is choosing between a prospect and its expected value, then for low probabilities—say, a choice between (0.05, 100; 0.95, 0) and 5 for sure—the DM prefers the prospect because the anticipated regret of *not* choosing the prospect and losing out on a larger amount (here, of 100) is greater. Yet for high probabilities—say, a choice between (0.95, 100; 0.05, 0) and 95 for sure—the DM prefers the EV because the anticipated regret of choosing the prospect, receiving nothing, and losing out on the sure amount (here, of 95) is greater. Figure 1 plots the CE under conditions F and N as well as the expected value.

Our example illustrates Proposition 1 and predicts an inverse-S curve for the certainty equivalents of the prospects under consideration. Because of the resolution premium, this curve is less linear when there is feedback. Given this example and



**Fig. 1** Expected value, Regret theory CEs under No feedback  $(CE_{RT_N})$  and Feedback  $(CE_{RT_F})$ 



Proposition 1, we make two summary predictions as follows. (i) When evaluating prospect  $x = (p, x_k; 1 - p, x_0)$ , a regret-averse decision maker is risk seeking for low probabilities of gains (p < 1/2) and risk averse for high probabilities (p > 1/2); (ii) the risk attitude of a regret-averse DM is reinforced in the presence of feedback owing to the resolution premium.

We tested these predictions in an experimental study. The next section is devoted to reporting the results of that study.

## 5 The experiment

Our experiment consisted of choices between prospects and was divided into two sections. Section I involved 24 questions devised for identifying regret-averse decision makers. The questions amounted to choices between two (three-outcome) prospects whose outcomes were determined by rolling a 6-sided die. Of these two prospects, one is clearly preferable to—and so should be chosen by—a regret-averse DM. In Section II of the experiment, another 26 questions were used to assess the risk attitudes of the regret-averse DMs identified in Section I. These latter questions were also choices between two prospects, but at this stage the outcomes were determined by rolling a 20-sided die. Much as in Section I, we expect that a particular one of the two prospects would be chosen by (and only by) a risk-averse decision maker. Each section of the experiment featured two conditions: with Feedback (condition F) and with No feedback (condition N). The experimental subjects were randomly assigned (in equal numbers) to one of these two conditions, both of which employed the exact same questions. In condition F, these subjects received immediate feedback about their payoff after each choice by rolling a 6- or 20-sided die (depending on the experiment's section). Immediately after the subject chose one of the prospects, a computer-simulated die was rolled and the subject was informed of the outcome. In condition N, subjects received no feedback after their choices.

We tested our predictions in terms of the following two hypotheses.

- H1: Regret-averse subjects are risk seeking for low probabilities (p < 1/2) and risk averse for high probabilities (p > 1/2) in conditions F and N both.
- H2: The risk attitudes of regret-averse subjects are reinforced more under condition F than under condition N.

The outcomes of prospects used in the experiment were small ( $\le 0 - \le 99$ ) and therefore within the domain of a decision maker's linear evaluation. This presumption allowed us to test both H1 and H2 for p < 1/2 and for p > 1/2.

### 5.1 Methodology

### 5.1.1 Subjects and stimuli

The computer-based experiment was conducted at the INSEAD–Sorbonne lab in Paris. The 107 subjects (71 female), of mean age 23, were university students in Paris. The stimuli used in each of the sections are shown in Appendix A. The Section I



stimuli (Fig. 3 in Appendix A) correspond to the monetary outcomes received under both prospects—outcomes that are determined by rolling a 6-sided die. In Section II of the experiment, the stimuli (Fig. 4 in Appendix A) again correspond to the monetary outcomes received under both prospects, but now those outcomes are determined by rolling a 20-sided die. The subjects were asked to express their preferences when comparing two prospects. Figure 5 in Appendix A depicts a (condition F) feedback value as indicated by the feedback device (6-sided die).

#### 5.1.2 Incentives

Each subject participating in the study was paid a flat fee of  $\in 8$ . To supplement that amount we instituted a randomized incentive procedure: subjects were informed that they might be able to play one of their randomly selected choices for real and win a cash amount of as much as  $\in 99$ . At the end of the experiment, 8 of the 107 subjects were randomly selected to play one of their choices for real. The selected subjects were asked to draw a question number from a box that consisted of all the questions used in the experiment. If the subject was in the Feedback condition, then she was paid the outcome originally given as immediate feedback for that particular question; if the subject was in the No feedback condition, then she rolled a 6- or 20-sided die. Thus the extra payouts were based on the subjects' original choices and a roll of the die. The average extra amount earned by these 8 randomly selected subjects was  $\in 25$ .

### 5.1.3 Procedures

Subjects were randomly assigned to one of the two experimental conditions and were informed that the experiment would take about 45 minutes to complete. The subjects were then given detailed instructions regarding the stimuli and the experiment, and they were also briefed about the incentive system. The instructions in both conditions were identical except that, in condition F, the subjects were told that they would know their payoff immediately after each choice. Both conditions used the same questions; the only difference between them was the presence of feedback.<sup>5</sup> The order of questions was randomized once, after which the same order was presented to all subjects.

The questions in Section I consisted of a choice between two prospects (see Table 16 in Appendix B). In each such pair, the "RA" prospect is the one that should be chosen by a regret-averse decision maker. Subjects were allowed to choose one of the two prospects or to express indifference; they were also informed that, if they expressed indifference between two prospects, then the computer would select one of them (with equal probability) on their behalf. In Section I, the subjects' responses to 16 of the 24 questions were used to identify regret-averse individuals. Of those 16 questions, 8 were choices between what we set up to be a regret-averse (RA) and a regret-seeking (RS) prospect of the same EV; the remaining 8 were choices between

<sup>&</sup>lt;sup>5</sup>The full list of questions is given in Appendix B (the instructions are available at goo.gl/jKOT3R and goo.gl/3ftKzu).



a RA and a RS prospect of different expected values. Six additional questions were used to estimate the *Q*-function parametrically; the Section I questions also included one to assess dominance and one to check for consistency. After answering the 24 questions in Section I of the experiment, all subjects proceeded to Section II.

In Section II of the experiment, subjects were required to choose between a less risky and a more risky prospect having the same expected value (see Table 17 in Appendix B). The presentation of less risky and more risky prospects was counterbalanced across questions. Monetary outcomes in Section II ranged from  $\leqslant$ 0 to  $\leqslant$ 50. Subjects were allowed to choose one of the prospects or to express indifference. The subjects' responses to 26 questions in Section II were used to identify risk attitudes. After answering the questions in Sections I and II, subjects were asked to provide personal and demographic information.

## 5.1.4 Validity of measurement

To ensure valid responses, we included dominance and consistency checks. These checks are detailed in what follows.

**Dominance checks** There were two dominance checks, one in each section of the experiment. The dominance checks were a choice between two prospects, one of which stochastically dominates the other. This check was included as question 11 in Section I and as question 14 in Section II.

Consistency checks These checks were included in the experiment to ensure consistent responses. One of the questions in each section was repeated (i.e., asked twice); thus, questions 8 and 17 (in Section I) were identical and questions 3 and 16 (in Section II) were identical.

### 5.1.5 Analyses

We first present data for the classification of subjects according to regret attitudes, after which to test hypotheses H1 and H2, we analyze the risk attitudes of regret-averse subjects. Differences between proportions were tested via binomial and multinomial methods, and the significance of differences was tested parametrically.

Analysis for Section I We classified subjects based on their regret attitudes. Removing the dominance and consistency checks left 22 questions, of which 16 allowed us to classify subjects according to their regret attitudes. For each of those 16 questions, a subject could choose the RA or the RS prospect or could express indifference. A subject who expressed indifference for the majority of questions was classified as regret neutral; one who chose the RA (resp., RS) prospect for the majority of questions was classified as regret-averse (resp., regret seeking). All subjects with no majority choice were classified as "mixed". As mentioned previously, in half of the 16 questions the RA prospect's EV was lower than that of the RS prospect. The



reason for including such questions is to control for the curvature of utility function at individual level.  $^6$ 

The remaining six questions in Section I allowed us to estimate parametrically the regret function Q under conditions F and N at the aggregate level and test if  $Q_F$  is more convex than  $Q_N$  (the assumption that underlies our hypotheses). We assume a linear utility function and a power function specification for the regret function:  $Q(\alpha) = \alpha^{\theta}$  if  $\alpha \geq 0$  and  $Q(\alpha) = -|\alpha|^{\theta}$  if  $\alpha < 0$ . The six questions were chosen such that they covered the range of  $\theta$  values [0.8, 2.4] observed in Bleichrodt and Diecidue (2010) and Baillon and Cillo (2015). The aggregate  $\theta$  estimated under conditions F and N allowed us to compute the resolution and regret premiums via (respectively) Eqs. 8 and 9.

Analysis for Section II Following the classification derived in Section I, we restricted our focus to regret-averse subjects. So in the results and analysis for Section II of the experiment, the term "subjects" refers to regret-averse subjects. After removal of the dominance and consistency checks there remained 23 questions, of which 16 were a choice between a risky prospect and a sure outcome. These 16 questions allowed us to classify subjects based on their risk attitudes. Just as with regret attitudes in Section I, a subject who expressed indifference for the majority of questions was classified as risk neutral; one who chose the safe (resp., risky) prospect for majority of questions was classified as risk averse (resp., risk seeking). As before, subjects with no majority choice were classified as "mixed". Because the 16 questions asked subjects to choose between a risky prospect and a sure outcome, the certainty effect (Kahneman and Tversky 1979; Cohen and Jaffray 1988) could affect their choices. To control for this effect, the remaining 7 questions in Section II were a choice between two risky prospects: a "low probability of a large outcome" prospect and a "high probability of a small outcome" prospect of the same expected value. These 7 questions allowed us to test H1 while controlling for the certainty effect. For each question, a subject could choose one of the risky prospects or express indifference. Note that the prospects we included in Section II, had the probability of positive outcomes in the range (0-0.3] or [0.7, 1). We did not include the intermediate range of probabilities to control for utility curvature (see discussion after Proposition 1 for details).

We divide the rest of our analysis of Section II into three levels: subject, question, and aggregate. Hypotheses H1 and H2 were tested at all three levels. For the first two levels, we classified (respectively) subjects' choices and the questions themselves as

<sup>&</sup>lt;sup>6</sup>A subject with a concave or convex utility function might prefer the RA prospect despite not being regret averse. For instance, consider a choice between prospects  $a = (E_1, 20; E_2, 70; E_3, 30)$  and  $b = (E_1, 45; E_2, 25; E_3, 50)$  when all three events are equally likely. Prospect a is a RA prospect because if Q is convex and u is linear then Q(45) > Q(25) + Q(20), in which case  $a \ge b$ . If instead u is convex and Q is linear, we still have  $a \ge b$ . Similar cases occur also when u is concave and Q is linear. To avoid classifying such subjects as regret averse, we included eight questions in which the RA prospect's EV was *lower* than that of the RS prospect.



Table 3	Classification of
experime	ental subjects based on
regret att	itudes

	Condition F	Condition N	
Regret averse	36 (67%)	49 (92%)	
Regret seeking	14 (26%)	3 (6%)	
Regret neutral	3 (6%)	_	
Mixed	1 (2%)	1 (2%)	

being either "consistent with H1", "inconsistent with H1", or "unclassified." In aggregate level, we consider all choices made by all subjects and check their consistency with H1.<sup>7</sup>

#### 5.2 Results

Of the 54 subjects in condition F, three violated the dominance check; in condition N there was no dominance violation. We performed the analysis both with and without those subjects and, since no significant differences were found, we include all the subjects in the following analysis.

#### 5.2.1 Section I

Table 3 shows, for each condition, the number (and percentage) of subjects classified in terms of their regret attitudes.

In both conditions, the majority of the subjects were regret averse: 67% in condition F and 92% in condition N. The proportion of regret-averse subjects was greater than the proportion of mixed subjects (p < 0.001) and regret-seeking subjects (p < 0.001) in both conditions, which indicates that—as one would expect—regret aversion is the dominant phenomenon. We also measured the proportion of regret-averse choices made by subjects: 67.5% in condition F and 82.8% in condition N. The difference is significant (p < 0.001), so Section I of the experiment offers solid evidence that feedback reduces regret aversion.

Estimation of regret and resolution premium: The role of feedback Six questions in Section I allowed for estimating the regret function Q under conditions F and N. In Table 4 we list the aggregate-level choices of subjects under both conditions for the six questions, where MRA denotes the more regret-averse prospect (on the left) and LRA the less regret-averse prospect (on the right). For each question, the exponent  $\theta$  that renders a decision maker indifferent between the MRA and LRA prospects is reported in the second column. The percentage of subjects choosing MRA and LRA under each condition is reported in the last four columns of the table.

Table 4 shows that, at the aggregate level, the majority choice shifts from MRA to LRA for a value of  $\theta$  between 1.3 and 1.6 under feedback and between 1.6 and 1.95

<sup>&</sup>lt;sup>7</sup>If more than 50% of choices are consistent with H1, we classify the subject and question as "consistent with H1." In case of indifference, we choose one of the options with equal probability.



Questions (MRA vs. LRA)	Indifference $\theta$	Condition l	F	Condition N		
		% MRA	% LRA	% MRA	% LRA	
(22, 96, 43) vs. (67, 1, 78)	0.8	78	17	96	4	
(99, 23, 35) vs. (9, 73, 75)	1	56	37	67	25	
(27, 32, 83) vs. (69, 78, 8)	1.3	56	39	75	25	
(89, 32, 18) vs. (9, 71, 73)	1.6	37	52	48	40	
(25, 93, 22) vs. (69, 18, 73)	1.95	33	50	27	58	
(35, 32, 73) vs. (79, 75, 15)	2.41	13	78	25	73	

**Table 4** Estimating  $\theta$  at the aggregate level—all experimental subjects

Boldface values indicate the switching point

MRA = more regret-averse prospect, LRA = less regret-averse prospect

under no feedback. We use this information to derive an aggregate  $\theta$  value of 1.45 (i.e., the midpoint between 1.3 and 1.6) under condition F; under condition N, we derive  $\theta=1.78$  (midpoint between 1.6 and 1.95). Hence the corresponding Q-functions under condition F and condition N are  $Q_F(\alpha)=\alpha^{1.45}$  and  $Q_N(\alpha)=\alpha^{1.78}$ , respectively. We observe that the Q-function under feedback ( $Q_F$ ) is less convex than the Q-function under no feedback ( $Q_N$ ); overall, then, immediate feedback reduces subjects' level of regret aversion. The estimated Q-function under condition N,  $Q_N(\alpha)=\alpha^{1.78}$ , is consistent with Bleichrodt and Diecidue (2010).

Next we shall estimate the Q-function of regret-averse subjects only. Table 5 lists the proportion of these subjects choosing MRA and LRA under conditions F and N. We observe that the majority choice shifts from MRA to LRA for  $\theta$  between 1.95 and 2.41 under feedback and between 1.6 and 1.95 under no feedback. Given this majority choice, we derive the Q-functions under conditions F and N as  $Q_F(\alpha) = \alpha^{2.16}$  and  $Q_N(\alpha) = \alpha^{1.78}$ , respectively. For these regret-averse subjects we observe that the Q-function under feedback ( $Q_F$ ) is *more* convex than the Q-function under no feedback ( $Q_N$ ); hence immediate feedback *increases* the regret aversion of subjects who are already regret averse.

From the results reported in Tables 3 and 4, we inferred that immediate feedback leads to less regret aversion (i.e., a less convex *Q*-function). For regret-averse subjects, however, the regret function is more convex under feedback than under no feedback (see Table 5). We also estimated *Q*-functions for regret-seeking subjects, which were the same in condition N as in condition F.<sup>8</sup> Thus feedback increases the number of regret-seeking subjects and thereby reduces the subject pool's overall

<sup>&</sup>lt;sup>8</sup>The estimated regret functions of regret-seeking subjects are identical under conditions F and N:  $Q_F(\alpha) = Q_N(\alpha) = \alpha^{0.9}$ . However, feedback increases the number of regret-seeking subjects. In particular, the number (14) of regret-seeking subjects in condition F is significantly larger than the number (3) of regret-seeking subjects in condition N. Feedback therefore decreases the entire subject pool's regret aversion. The extremely few regret-seeking subjects under condition N precludes any meaningful comparison with their counterparts under condition F.



Questions (MRA vs. LRA)	Indifference $\theta$	Condition I	F	Condition N		
		% MRA	% LRA	% MRA	% LRA	
(22, 96, 43) vs. (67, 1, 78)	0.8	89	8	98	2	
(99, 23, 35) vs. (9, 73, 75)	1	75	19	72	21	
(27, 32, 83) vs. (69, 78, 8)	1.3	69	25	77	23	
(89, 32, 18) vs. (9, 71, 73)	1.6	56	33	56	33	
(25, 93, 22) vs. (69, 18, 73)	1.95	44	39	28	58	
(35, 32, 73) vs. (79, 75, 15)	2.41	19	72	26	74	

**Table 5** Estimating  $\theta$  at the aggregate level—regret-averse subjects only

Boldface values indicate the switching point

MRA = more regret-averse prospect, LRA = less regret-averse prospect

regret aversion. At the same time, feedback increases the regret aversion of regretaverse subjects. In short, feedback polarizes regret attitudes: subjects who are regret averse or regret seeking become even more so when feedback is given.

In the analysis that follows, we once again focus solely on regret-averse subjects. Our previous estimates of the exponent  $\theta$  for regret-averse subjects enables measurement of the two components of risk premium under regret theory. As a concrete example, in Table 6 we report the resolution and regret premiums of the prospect  $(p_j, 50; 1 - p_j, 0)$  computed for different probabilities  $p_j$  using Eqs. 8 and 9, respectively.

In Fig. 2 we plot the estimated certainty equivalent under condition F and condition N. H1 states that—under both conditions—a decision maker is risk seeking for low probabilities of gains (p < 0.5) and risk averse for high probabilities (p > 0.5). Since immediate feedback increases the regret aversion of a regret-averse DM (makes his Q-function more convex), it follows that the DM should be more risk seeking (resp., risk averse) for low (resp., high) probabilities in condition F than in condition N; this is hypothesis H2. Thus, our results from Section I validate the assumptions about regret attitudes that underlie our hypotheses. We next discuss the validity of H1 and H2 in Section II of the experiment.

**Table 6** Resolution premium and regret premium under conditions F and N

Probability	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
Resolution premium	-2	- 1.51	- 0.99	- 0.49	0	0.49	0.99	1.51	2
Regret premium	-6.27	-5.72	-4.15	-2.16	0	2.16	4.15	5.72	6.27
Expected value	5	10	15	20	25	30	35	40	45
CE (condition N)	11.27	15.72	19.16	22.16	25	27.83	30.84	34.27	37.83
CE (condition F)	13.27	17.23	20.15	22.65	25	27.34	29.85	32.76	35.83
Total risk premium	-8.27	-7.23	-4.16	-2.65	0	2.65	4.16	7.23	8.27



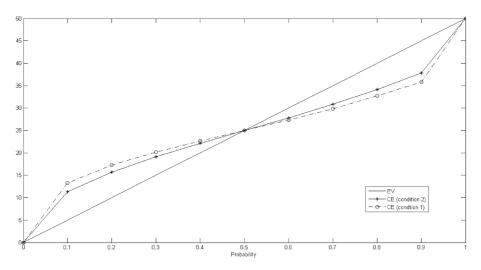


Fig. 2 Certainty equivalent under conditions F and N for the estimated value of  $\theta$ 

#### 5.2.2 Section II

We now present results concerning the risk attitudes of regret-averse subjects. There were 36 (67%) such subjects in condition F and 49 (92%) in condition N. The classification of regret-averse subjects based on risk attitude is described in the Online Appendix F. Predominantly, regret-averse subjects were risk averse in both the conditions. We now test the risk attitudes of regret-averse subjects (hypotheses H1 and H2) at the subject level, the question level, and the aggregate level.

**Subject-level results** We employed two sets of questions for the measurement of risk attitude. In questions from the first set we provided each subject the choice between a risky prospect and its expected value. For this first set of questions, Table 7 reports the number (and percentage) of subjects who are—with respect to H1—consistent, inconsistent, and unclassified. The proportion of subjects consistent with H1 was 56% in condition F and 63% in condition N, but that difference is not significant. We observe that, in both conditions, a higher percentage of subjects are consistent than inconsistent with H1. However, this difference is not significant either in condition F (p = 0.24) or in condition N (p = 0.06).

In questions from the second set we provided subjects with a choice between two risky prospects: a "low probability of a large outcome" prospect and a "high

**Table 7** Classification of subjects based on consistency with H1—**first set** of questions

	Condition F	Condition N
Consistent with H1	20 (56%)	31 (63%)
Inconsistent with H1	13 (36%)	18 (37%)
Unclassified	3 (8%)	0 (0%)



Table 8 Classification of
subjects based on consistency
with H1—second set of
questions

	Condition F	Condition N
Consistent with H1	8 (22%)	6 (12.2%)
Inconsistent with H1	27 (75%)	41 (83.6%)
Unclassified	1 (3%)	2 (4%)

probability of a small outcome" prospect of the same expected value. According to H1, a regret-averse subject should prefer the "low probability of a large outcome" prospect. For this second set of questions, Table 8 reports the number of subjects who are consistent or inconsistent with H1 (or unclassified). The proportion of subjects whose choices were consistent with H1 was only 22% in condition F and 12.2% in condition N—significantly smaller, in both conditions, than those of the subjects who are *inconsistent* with H1. Clearly, then, participant responses to the second set of questions run counter to that hypothesis.

**Question-level results** As just discussed, we used two sets of questions to measure risk attitudes. Table 9 lists the proportion of subjects choosing between a risky prospect and its expected value. For each of the 16 questions, Table 9 gives the choice

Table 9 Percentage of subjects making choices that are consistent vs. inconsistent with H1—risky prospects vs. their expected values

		Condition F		Condition N		
Question choices	Prediction of H1	Proportion ch	noosing	Proportion choosing		
		Prospect A	Prospect B	Prospect A	Prospect B	
(0.8, 40; 0) vs. 32	В	31%	67%**	14%	84%**	
(0.95, 50; 0) vs. 47.5	В	42%	56%	27%	69%**	
(0.05, 50; 0) vs. 2.5	A	53%	42%	37%	57%	
(0.3, 40; 0) vs. 12	A	19%	78%**	6%	88%**	
(0.1, 40; 0) vs. 4	A	47%	53%	24%	67%**	
(0.7, 50; 0) vs. 35	В	36%	58%	14%	84%**	
(0.15, 40; 0) vs. 6	A	22%	72%**	22%	68%**	
(0.75, 40; 0) vs. 30	В	14%	81%**	8%	92%**	
(0.2, 50; 0) vs. 10	A	19%	75%**	14%	78%**	
(0.85, 50; 0) vs. 42.5	В	28%	72%**	16%	82%**	
(0.9, 40; 0) vs. 36	В	36%	64%*	14%	84%**	
(0.25, 50; 0) vs. 12.5	A	19%	78%**	18%	78%**	
(0.9, 5; 0) vs. 4.5	В	13%	87%**	11%	86%**	
(0.05, 8; 0) vs. 0.4	A	61%**	29%	69%**	14%	
(0.1, 5; 0) vs. 0.5	A	65%**	29%	75%**	14%	
(0.95, 8; 0) vs. 7.6	В	26%	74%**	14%	81%**	

Payoffs for responses to questions (i.e., subjects' choices) are denominated in euros ( $\in$ ). Boldface indicates that the majority of responses to that question were consistent with H1. \*significant at  $\alpha=10\%$ , \*\*significant at  $\alpha=5\%$ , \*\*\*significant at  $\alpha=1\%$ 



**Table 10** Classification of questions based on majority choices with respect to H1

	Condition F	Condition N
Consistent with H1	11	10
Inconsistent with H1	5	6
Unclassified	0	0

predicted by H1, the majority choice, and the proportion of subjects choosing the prospect that is consistent with H1. Table 10 summarizes results concerning the number of questions for which the majority of subject responses is consistent with H1. For 10 out of 16 questions the majority choice was consistent with H1 in condition N; in condition F, the majority choice was consistent with H1 for 11 out of 16 questions. The other questions were all inconsistent with H1.

For each question, we tested whether the proportion of choices consistent with H1 is different from the proportion of choices inconsistent with H1; Table 11 presents the results. At the 95% confidence level, under condition F we found that 7 questions were consistent with H1, 4 were inconsistent with H1, and the other 5 questions were unclassified; under condition N, 10 (resp. 5) questions were consistent (resp. inconsistent) with H1 and the remaining question was unclassified. So overall, subject responses to the first set of questions support H1 under condition N and—even more strongly—under condition F.

We also tested hypothesis H1 using the second set of questions, which asked subjects to choose between two risky prospects: a "low probability of a large outcome" prospect and a "high probability of a small outcome prospect" of the same expected value. To be consistent with H1, subjects should prefer the "low probability of a large outcome" prospect. Table 12 lists the prospects and the proportion of subjects choosing each. Except for one question in condition 1, we find no support for H1 in the responses to these questions.<sup>9</sup>

Much as with the subject-level results, we observe that majority choices for most of the questions are consistent with H1 when subjects are asked to choose between a risky prospect and its expected value. However, if subjects are asked to choose between two risky projects—one offering a less probable high payoff and the other a more probable low payoff—then participant choices are inconsistent with H1. We conclude that there is no evidence in favor of H1 at the question level of analysis.

**Aggregate-level results** Table 13 shows that the majority of choices were consistent with H1—both in condition F (53.4%) and in condition N (56.5%). We found that in both conditions the subjects were risk averse for both low and high probabilities of gains. We conclude that, although more than 50% of the choices were consistent with H1, we do not find evidence of risk seeking for small probabilities.

<sup>&</sup>lt;sup>9</sup>If the certainty effect influenced our result, then the subjects would have been more consistent with respect to H1 for the *second* set of questions (since both prospects are risky). However, our evidence points in the opposite direction.



	Condition F		Condition N			
	$\alpha = 0.05$	$\alpha = 0.1$	$\alpha = 0.05$	$\alpha = 0.1$		
Consistent with H1	7	8	10	10		
Inconsistent with H1	4	4	5	5		
Unclassified	5	4	1	1		

Table 11 Classification of questions based on consistency with H1 and significance of proportions

**Table 12** Percentage of subjects making choices that are consistent vs. inconsistent with H1—two risky prospects (less probable high payoff vs. more probable low payoff)

		Condition F		Condition N			
Question choices	H1 prediction	Proportion c Prospect A	hoosing Prospect B	Proportion choosing Prospect A Prospect B			
(0.3, 40; 0) vs. (0.8, 15; 0)	A	17%	72%**	8%	80%**		
(0.1, 45; 0) vs. (0.9, 5; 0)	A	42%	56%	18%	73%**		
(0.1, 40; 0) vs. (0.8, 5; 0)	A	33%	58%	20%	63%**		
(0.05, 50; 0) vs. (0.85, 3; 0)	A	50%	42%	33%	55%		
(0.15, 50; 0) vs. (0.75, 10; 0)	A	22%	78%**	10%	80%**		
(0.2, 40; 0) vs. (0.8, 10; 0)	A	14%	78%**	10%	78%**		
(0.25, 40; 0) vs. (0.8, 12.5; 0)	A	22%	69%**	14%	73%**		

See Notes to Table 9

**Table 13** Choices consistent with H1 at the aggregate level

Questions	Choices consistent with H1	Risk attitude
Condition F		
p < 1/2	104 out of 278 (37.4%***)	Risk aversion
p > 1/2	193 out of 278 (69.4%***)	Risk aversion
Total	297 out of 556 (53.4%*)	Consistent with H1
Condition N		
p < 1/2	112 out of 366 (30.6%***)	Risk aversion
p > 1/2	302 out of 366 (82.5%***)	Risk aversion
Total	414 out of 732 (56.5%***)	Consistent with H1



<sup>\*</sup>significant at  $\alpha = 10\%$ , \*\*\*significant at  $\alpha = 1\%$ 

**Table 14** Aggregate-level choices between less probable high payoffs and more probable low payoffs

***significant at $\alpha = 1\%$	***si	gnificant	at α	=	1%
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Conditions	Consistent with H1	Inconsistent with H1
Condition F	26%	66%***
Condition N	16%	71%***

We also tested H1 by comparing the proportion of subjects choosing the "low probability of a large outcome" prospect over the "high probability of a small outcome" prospect. Table 14 reveals that the choices of most subjects were inconsistent with H1. Thus we find no evidence in favor of H1 at the aggregate level, either.

To validate H2, we compared the proportion of choices consistent with H1 in condition F versus condition N. Table 15 presents the results, which indicate that—in line with our prediction—regret-averse subjects are more risk seeking for *low* probabilities under feedback. Yet for high probabilities also we find that, contrary to our prediction, increased risk seeking under feedback. When all questions are considered, the evidence in favor of H2 is neither significant nor persuasive. The subjects become uniformly more risk seeking under Feedback than under No feedback.

The analysis of Section II focuses only on risk attitudes of regret-averse subjects. However, to fully understand the effect of feedback on risk attitudes, we consider the entire sample that includes regret neutral and regret seeking subjects. Online Appendix E reports the full analysis. In sum, under condition N, given that regret-averse subjects form 92% of the sample, the results described for regret-averse subjects (in Tables 13 and 15) and the entire subject pool are identical. Under condition F, as 33% of the subjects are regret seeking or neutral, the risk attitudes of "regret-averse" subjects and the "entire sample" differ. The comparison of Table 15 with Table 19 in Online Appendix E shows that the "entire sample" and "regret averse" subjects are globally risk averse and feedback increases risk seeking for low and high probabilities. However, under feedback, the "entire sample" is more risk seeking for probabilities p > 0.5 than "regret averse" subjects. To further explore, we looked at the risk attitudes of subjects who are *non regret averse* (see Tables 20 and 21 in Online Appendix E): Under condition F the non regret-averse subjects

Table 15 Effect of feedback (resolution premium) at the aggregate level and across all choices—regretaverse subjects

	Proportion cons	istent with H1		
Choice	Condition F	Condition N	Difference	Effect of feedback
p < 1/2	37.4%	30.6%	6.8%*	Increased risk seeking
p > 1/2 Total	69.4% 53.4%	82.5% 56.5%	-13.1%** $-3.1%$	Reduced risk aversion Reduced consistency with H1

<sup>\*</sup>significant at  $\alpha = 10\%$ , \*\*significant at  $\alpha = 5\%$ 



are risk averse for low probabilities (p < 0.5) and risk seeking for high probabilities (p > 0.5). This behavior of non regret-averse subjects is consistent with regret theory's prediction under concave Q.

We also conducted an extensive online pilot study (on the Socialsci platform). The 121 subjects (64 female, mean age = 31.6) were Americans representing all income levels. Results of the lab experiment reported in this paper replicated, by and large, those of the pilot. In both studies: (i) regret aversion was the dominant phenomenon under both conditions; (ii) there was support for H1 at the subject, question, and aggregate level for the first set of questions under both conditions; and (iii) feedback increased the risk-seeking attitudes of regret-averse subjects for both small and large probabilities. In the pilot we were able to check the robustness of results to payoff levels lower than those used in Section II of this experiment. The detailed pilot results are available upon request.

### 6 Discussion and conclusions

The paper presents an analysis of risk attitudes under regret theory. We derive analytical expressions for the risk premium's two components under that theory: the resolution premium and the regret premium. We also empirically estimate those two components and characterize the risk attitude of a regret-averse decision maker. That characterization yields two predictions that we test in an experiment. We find that regret aversion is a robust phenomenon. The estimates for the parameter of the regret function Q were also in accordance with findings reported in Bleichrodt and Diecidue (2010). Our consistent results across two experiments (lab study and online pilot) for a total of 228 subjects lend credence to regret theory and to our experimental methodology.

We find mixed support for the risk attitudes predicted by regret theory. We observe that our results are consistent with H1 when the choice is between a prospect and a sure outcome. However, we do not find support for H1 when subjects must choose between two prospects of the same expected value (a "low probability of a large outcome" prospect and a "high probability of a small outcome" prospect). Because responses to the second set of questions could not be confounded by a certainty effect (since there was no sure outcome), we expected them to offer more support for H1. However, we found almost no support for H1 in the second set of questions under either condition: irrespective of feedback, subjects preferred (to a significant degree) a more probable low payoff over a less probable high payoff. The support for H1 in the first set of questions and the absence of that support in the second set is surprising, and it suggests that a different mechanism could be operating in response to the two sets of questions. For example, subjects could have attended more to probabilities in the second than in the first set of questions; that emphasis could have triggered a comparison (regret versus rejoicing) on the probability scale rather than on the outcome scale, resulting in choices that are inconsistent with H1. The role of probability



attention and probability transformation has been extensively studied in decision theory. Since regret theory captures comparisons only on the outcome scale and ignores comparisons on the probability scale, it may not always predict risk attitudes accurately. The above argument is also supported by the data: In Online Appendix G, we compare the predictions of regret theory with another popular alternative to expected utility that transforms probabilities i.e, prospect theory. We find that, for intermediate probabilities  $p \in (0.1, 0.5]$ , prospect theory with an inverse-S probability weighting fits the data better than regret theory. Therefore, further development and investigation is needed of models that can capture anticipated regret on both probability and outcome scales; one example is the perceived relative argument model, or PRAM (Loomes 2010).

The other explanation for the lack of support for regret theory's risk attitude predictions is that we used three-outcome prospects to identify regret averse DMs (Section I), but two-outcome prospects to test their risk attitudes (Section II). Theoretically this should not matter, but decreasing the number of outcomes changes the state space and could have made outcome comparisons difficult (Baillon et al. 2015 also face a similar issue). Additionally, in Section II stimuli (for both set of questions), we were not able to make outcome comparisons distinct. For example to trigger outcome comparisons in the first set of questions, we were not able to split the single outcome of the safe prospect into two separate outcomes coinciding with the risky prospect's state space—as the event splitting effect (Starmer and Sugden 1993) could affect the results.

Our experiment also provides new insights regarding the effect of feedback on regret and risk attitudes. It is assumed in most of the psychology literature (Josephs et al. 1992; Larrick 1993; Larrick and Boles 1995; Ritov and Baron 1995; Ritov 1996; Zeelenberg et al. 1996) that people are generally regret averse and that feedback about foregone options increases regret aversion. In contrast, our results indicate that a significant number of subjects were actually regret seeking when there is feedback about payoffs. We observe that, although immediate feedback reduces the regret aversion of the entire subject pool, it increases the regret aversion of regret-averse subjects, <sup>10</sup> thus validating the assumptions that underlie our hypothesis H2. Our results also emphasize that the effect of feedback on anticipated regret is less straightforward than its treatment in the psychology literature suggests. Because our study does not employ a within-subject design, we cannot ascertain precisely how feedback influences subjects exhibiting various degrees of regret aversion. Nonetheless, the results presented here provide the first evidence that feedback may affect subjects differently depending on their prior attitude toward regret. Future research should provide more insights on how prior regret attitude moderates the effect of feedback on regret attitudes.



 $<sup>^{10}</sup>$ When subjects whose responses in Section II were inconsistent with regret theory are removed and the Q-function is then recomputed, we still find that feedback polarizes regret attitudes.

We were also able to measure the effect of feedback for the first time in the literature: We empirically estimated the resolution premium and thereby quantified the psychological pain (and pleasure) of immediate feedback. In other words, we were able to estimate precisely how much more a decision maker would pay for a risky prospect when she expects to receive immediate feedback. This estimation has the potential to allow deployment of regret theory for applications in public policy, marketing, and investment. For example, the resolution premium accounts for why a regret-averse investor prefers betting on the underdog in a sport competition (i.e., feedback) to investing in a start-up venture of equal worth (delayed or no feedback).

The results reported in this paper also help us understand the effect of feedback on the risk attitudes of regret-averse DMs. Regret theory predicts that if feedback increases an individual's regret aversion then it should reinforce his risk attitude (H2). Although the regret aversion of regret-averse subjects did increase under feedback in our experiment, we do not find statistical support for H2. In our experiment (and also in the pilot study), regret-averse subjects are significantly more risk-seeking for both low and high probabilities of gains. However, interestingly we find that non regretaverse subjects behave consistently with regret theory under feedback. Thus it seems that anticipated regret could be one of the many mechanisms that moderates the effect of feedback on risk attitudes. The literature on decision from experience (Barron and Erev 2003; Hertwig et al. 2004; Erev et al. 2017) provides additional evidence concerning the effect of feedback on attitudes toward risk. In a recent paper, consistent with our results, Erev et al. (2017) find that feedback instigates regret minimizing choices, but increases risk seeking for gains. They suggest different mechanisms (like the change in shape of the probability weighting function, reliance on a small sample) that could mediate the effect of feedback on risk attitudes. Future research should compare such alternatives with the mechanism (explored in this paper) of anticipated regret. Doing so would increase still further our knowledge about the role of immediate feedback in affecting risk attitudes.

By modeling the risk attitudes under regret theory and measuring the resolution and regret premium empirically, we show that regret theory is a simple yet powerful framework to describe the pervasive emotion of regret and the risk attitudes associated. However our experimental results suggest that regret theory provides a partial account of risk attitudes as it captures the regret-rejoicing trade-offs on the outcome scale only. As a consequence, decision analysts can effectively use regret theory to understand the effects of anticipated regret and feedback on the outcome scale. Decision theorists should target their efforts in developing new models to capture the regret-rejoicing trade-offs also on the probability scale.

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## Appendix A

## Example of experimental stimuli for Sections I and II

Question 2: Choose between A and B (Note that the numbers 1,2,.....,6 in the figure below are obtained by rolling the six sided dice)

Choice	1	2	3	4	5	6	
Α	\$ 30		\$	50	\$ 5		
В	\$ 10		\$	30	\$ 4	45	

#### Which one do you choose? \*

- Option A
- Option B
- Equally prefer option A and B

Fig. 3 Screenshot of Section I stimuli

Question 1: Choose between A and B (Note that the numbers 1,2,.....,20 in the figure below are obtained by rolling the twenty sided dice)

Choice	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
А	\$ 20	\$0																		
В	\$1																			

#### Which do you choose? \*

- Option A
- Option B
- Equally prefer option A and B

Fig. 4 Screenshot of Section II stimulii

The dice below was rolled and it showed "3", so you receive 80.You would have received 8 if you had chosen option B.



Fig. 5 Screenshot of feedback

# Appendix B

# Questions used in Sections I and II of the lab experiment

Table 16 Questions used in Section I of the lab experiment

Three-outcome prospects	Choice of regret-averse DM	
(each outcome equally likely)	(RA prospect)	Question design
(35, 80, 40) vs. (75, 8, 72)	Option A	Same EV
(30, 50, 5) vs. (10, 30, 45)	Option B	Same EV
(64, 6, 60) vs. (20, 90, 20)	Option B	Same EV
(15, 55, 65) vs. (80, 25, 30)	Option B	Same EV
(58, 55, 40) vs. (3, 80, 70)	Option A	Same EV
(9, 70, 75) vs. (99, 30, 25)	Option B	Same EV
(30, 40, 50) vs. (20, 30, 35)	Dominance	
(5, 50, 45) vs. (55, 25, 20)	Option B	Same EV
(20, 25, 80) vs. (55, 69, 1)	Option A	Same EV
(50, 6, 55) vs. (20, 64, 25)	Option B	Different EV
(62, 40, 45) vs. (3, 71, 75)	Option A	Different EV
(74, 81, 4) vs. (30, 42, 86)	Option B	Different EV
(6, 76, 61) vs. (60, 48, 33)	Option B	Different EV
(34, 75, 23) vs. (69, 7, 58)	Option A	Different EV
(23, 18, 46) vs. (43, 38, 8)	Option A	Different EV
(53, 29, 25) vs. (4, 49, 55)	Option A	Different EV
(70, 50, 2) vs. (30, 20, 71)	Option B	Different EV
(6, 76, 61) vs. (60, 48, 33)	Option B	Consistency check
(99,23,35) vs. (9, 73, 75)	Indiff. for $\theta = 1$	Measure Q function
(22, 96, 43) vs. (67, 1, 78)	Indiff. for $\theta = 0.8$	Measure Q function
(27, 32, 83) vs. (69, 78, 8)	Indiff. for $\theta = 1.3$	Measure Q function
(89, 32, 18) vs. (9, 71, 73)	Indiff. for $\theta = 1.6$	Measure $Q$ function
(25, 93, 22) vs. (69, 18, 73)	Indiff. for $\theta = 1.95$	Measure $Q$ function
(79, 75, 15) vs. (35, 32, 73)	Indiff. for $\theta = 2.41$	Measure Q function

Payoffs for responses to questions are denominated in euros ( $\leqslant$ ). EV = expected value

**Table 17** Questions used in Section II of the lab experiment to identify attitudes toward risk

Question choices	Prediction of H1
(0.8, 40;0) vs. 32	В
(0.95, 50;0) vs. 47.5	В
(0.05, 50;0) vs. 2.5	A
(0.3, 40; 0) vs. 12	A
(0.1, 40; 0) vs. 4	A
(0.7, 50; 0) vs. 35	В
(0.15, 40; 0) vs. 6	A



Table 17   (continued)	Question choices	Prediction of H1
	(0.75, 40; 0) vs. 30	В
	(0.2, 50; 0) vs. 10	A
	(0.85, 50; 0) vs. 42.5	В
	(0.9, 40; 0) vs. 36	В
	(0.25, 50; 0) vs. 12.5	A
	(0.9, 5; 0) vs. 4.5	В
	(0.05, 8; 0) vs. 0.4	A
	(0.1, 5; 0) vs. 0.5	A
	(0.95, 8; 0) vs. 7.6	В
	(0.3, 40; 0) vs. (0.8, 15; 0)	A
	(0.1, 45; 0) vs. (0.9, 5; 0)	A
	(0.1, 40; 0) vs. (0.8, 5; 0)	A
	(0.05, 50; 0) vs. (0.85, 3; 0)	A
	(0.15, 50; 0) vs. (0.75, 10; 0)	A
Payoffs for responses to	(0.2, 40; 0) vs. (0.8, 10; 0)	A
questions are denominated in euros (€)	(0.25, 40; 0) vs. (0.8, 12.5; 0)	A

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